

Breve introducción a la computación cuántica

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27 de marzo de 2025

Miguel Cordon · 11 May 2020 · 2 min read

Singapore quantum computing startup Entropica Labs bags \$1.8m in seed funding



Founders of Entropica Labs (from left): Tommaso Demarie, Ewan Munro, and Joaquin Keller / Photo credit: Entropica Labs

 > quant-ph > arXiv:2007.14044

Quantum Physics

[Submitted on 28 Jul 2020]

Polyadic Quantum Classifier

[William Cappelletti](#), [Rebecca Erbanni](#), [Joaquín Keller](#)

We introduce here a supervised quantum machine learning algorithm that takes as input a dataset and outputs a specific bit string corresponding to the class of the input. The algorithm shows good accuracy --compared to a classical machine learning algorithm-- on a dataset. Furthermore, we evaluate with simulations how the algorithm performs on a larger dataset.

History

1981:

Richard Feynman — *Simulating Physics with Computers*, «*Nature is quantum, dammit!*»

1985:

David Deutsch — *Quantum Theory, the Church-Turing Principle and the Universal Quantum Computer*

1992:

Deutsch–Jozsa algorithm (theoretical result, no direct application)
Exponentially faster than any possible classical algorithm

1994:

Peter Shor's algorithm for integer factorization (breaks RSA cryptography)
Exponentially faster than any known classical algorithm

How faster ?

breaking (factoring) a 2048-bit RSA key

Classical Computing

Quantum Computing

Best classical algorithm:

Shor's quantum algorithm:

10^{34} steps
1 billion years

on El Capitan supercomputer

- 1.8 exaFLOPS
- 1M CPU - 10M GPU cores
- 10Mx faster than a gaming PC

How faster ?

breaking (factoring) a 2048-bit RSA key

Classical Computing

Best classical algorithm:

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1 billion years

on El Capitan supercomputer

- 1.8 exaFLOPS
- 1M CPU - 10M GPU cores
- 10Mx faster than a gaming PC

Quantum Computing

Shor's quantum algorithm:

10^7 steps
8 hours

on a quantum computer

- 20M physical qubits
- 1M Qops/s per qubit
- (superconducting qubits)

Work in progress... doable in 2030?

Hardware now

(physical qubits)

1998: First quantum computer: 2-qubit

2000: 7-qubit

2006: 12-qubit

2017: IBM 17-qubit, Rigetti 19-qubit, Google 22-qubit

2018: IBM 50-qubit, Google 72-qubit, ionQ 79-qubit

2022: IBM 433-qubit, Pasqal 300-qubit

2023: IBM 1121-qubit

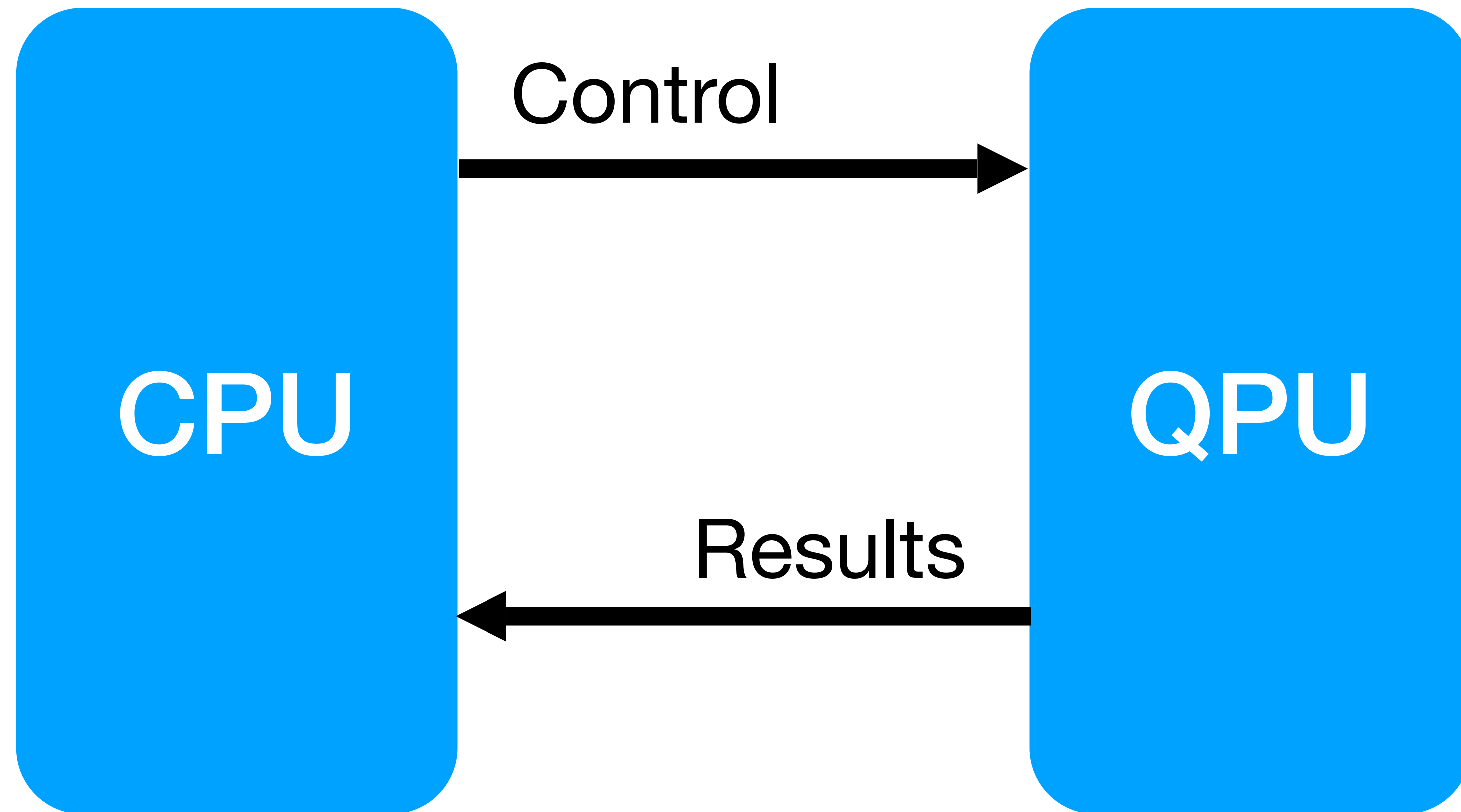
Physical vs logical qubits

- Physical, real qubits are noisy
- With error correction 1000 physical qubits
=> 1 logical qubit
- QPU power is determined by:
 - number qubits
 - error rate
 - qubit connectivity

Quantum computers are not faster classical computers

- They compute in a different way, the algorithms are different
- They can solve some problems exponentially faster — $O(n)$ vs $O(2^n)$
- We don't know which problems
- We don't now how

Hybrid Architecture



Cryptography and quantum computing

- «Quantum cryptography»
 - Quantum key distribution
- Post-quantum cryptography
 - Quantum-safe cryptography
- Quantum computers will break RSA

It's hard

- Software
 - Quantum computers are alien
 - Hard to make them compute something at all
 - Even harder to make them compute something useful
 - But useful is not enough....
 - It needs to be useful, and faster than classical computers
 - We don't have quantum computers to try stuff, to debug, to learn
- Hardware engineering
 - Qubits need to be isolated to exist
 - Qubits need to be manipulated to compute
 - Qubits are inherently unstable

Hardware roadmap (2020)

Google: a thousand error-corrected qubits “within the decade”

IBM: 4158+ physical qubits in 2025

IonQ: 1028 logical (error-corrected) qubits in 2028

PsiQuantum: 1 million of physical qubits by 2030

~1000 “physical” (noisy) qubits → one “logical” (corrected) qubit

Hardware paths

- Superconducting: Google, IBM, Rigetti, Alibaba
- Trapped ion: ionQ, Quantinuum (Honeywell), AQT, Universal Quantum, Huayi Boao
- Photonic: Xanadu, PsiQuantum, Jiuzhang
- Cold atoms: Pasqal, ColdQuanta, QuEra, Atom
- Cat qubits: Amazon, Alice&Bob
- Majorana: Microsoft — Spin qubits: Silicon Quantum Computing — ...

Potential applications (quantum advantage)

Cryptography: break RSA **ok**

Chemistry and material sciences: Quantum simulation **maybe**

Optimization: Logistics, finance **maybe not**

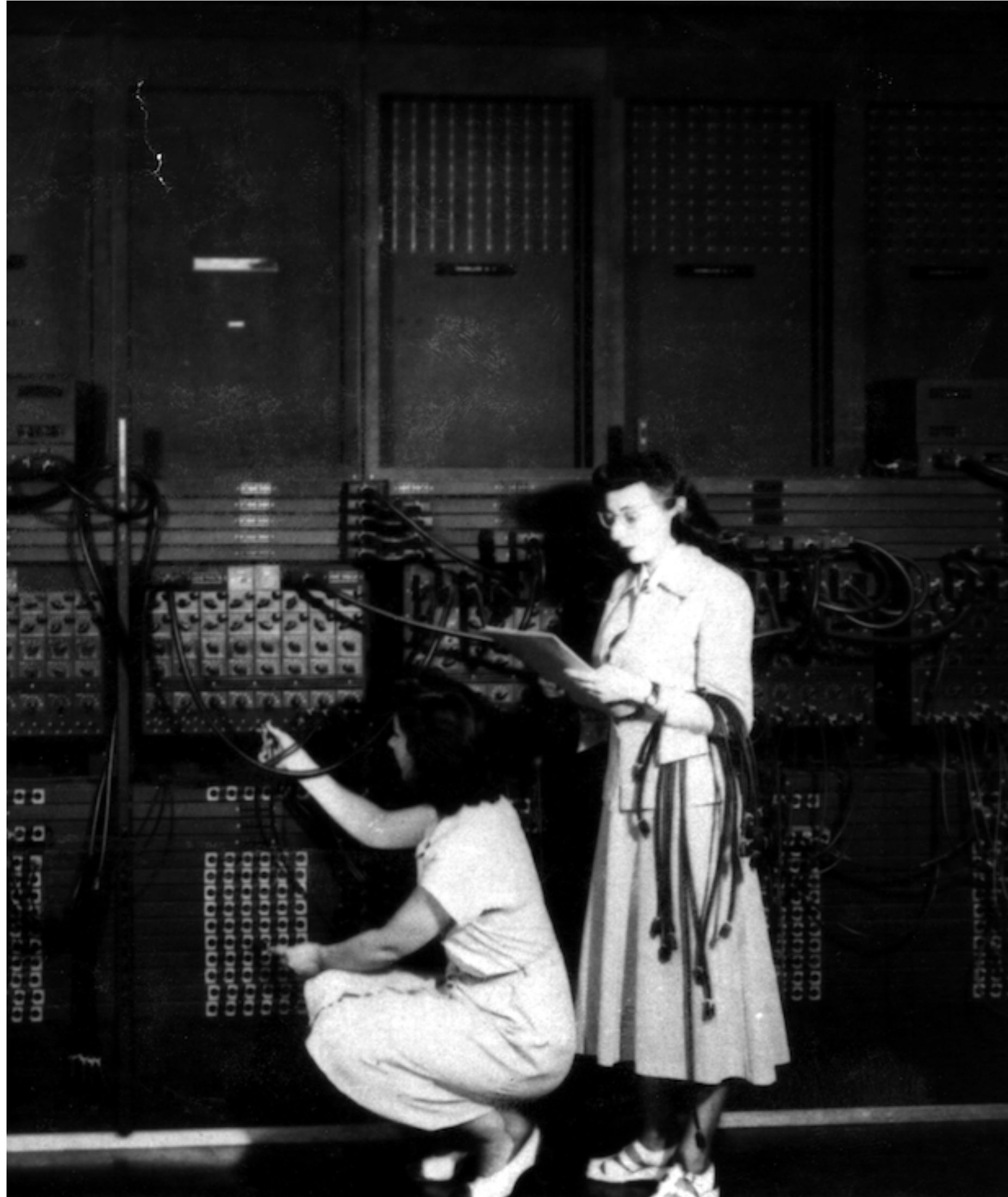
Quantum Machine Learning:

classical ML is already very good **maybe**

Skills for quantum computing

- Tensor algebra
- Statistics
- Theoretical Computer Science
- Programming
- Elements of quantum physics

1946

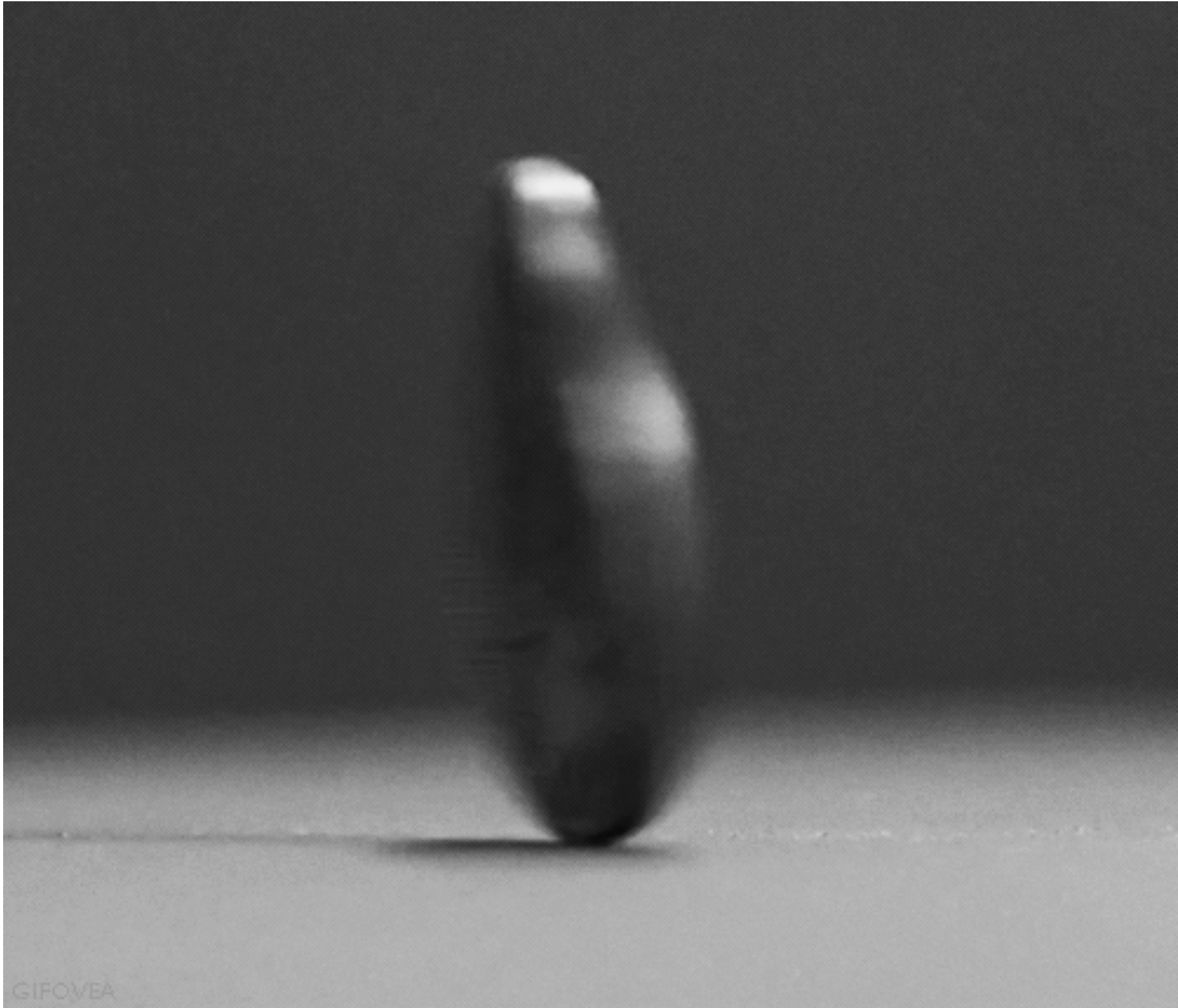


2016



Qubit

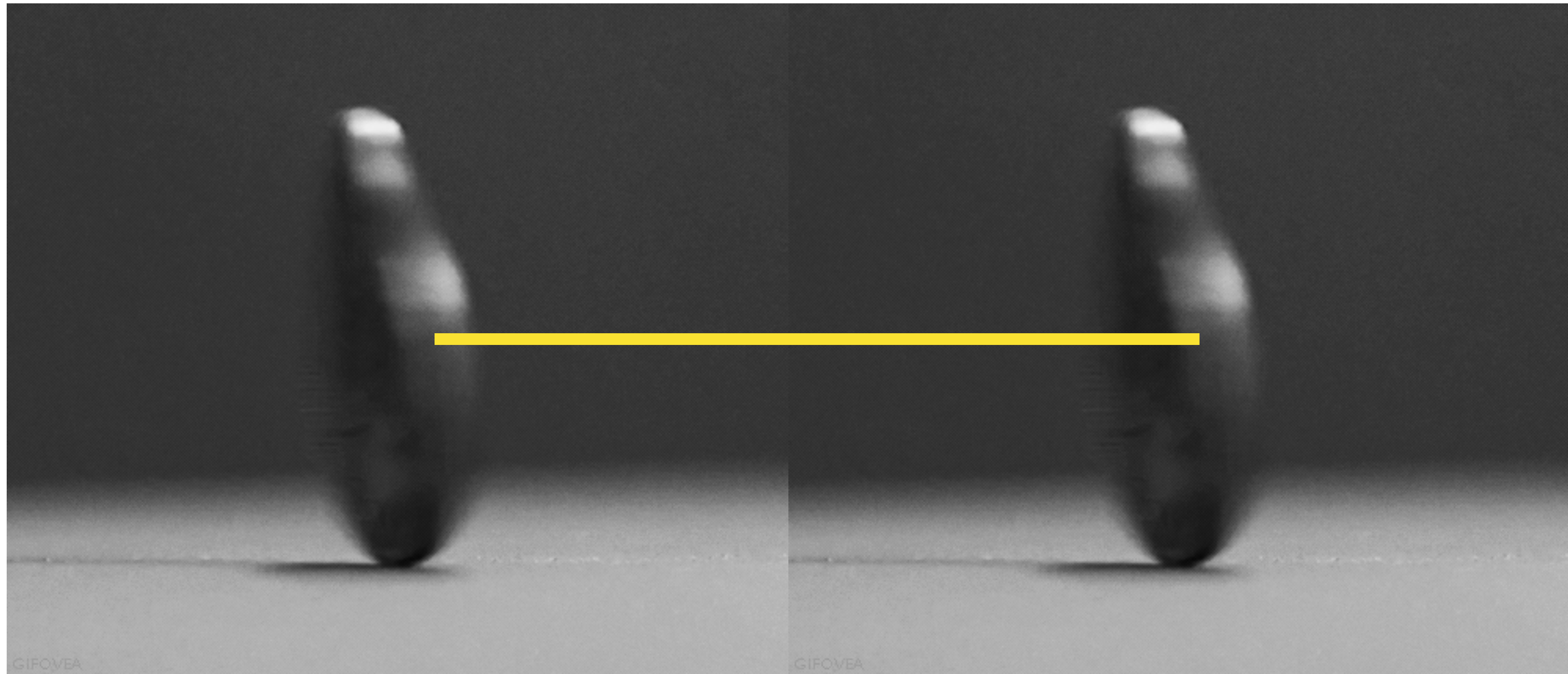
0



Measurement

1

Entangled Qubits



Entangled Qubits



Quantum state

1-qubit

$$a_0 \quad 0$$

$$a_1 \quad 1$$

a_0, a_1 are probability 'amplitudes'

amplitudes are complex numbers

$$a_0, a_1 \in \mathbb{C}$$

Probability from amplitude: $p = |a|^2$

'Duality wave/particle'

The 2-slit experiment

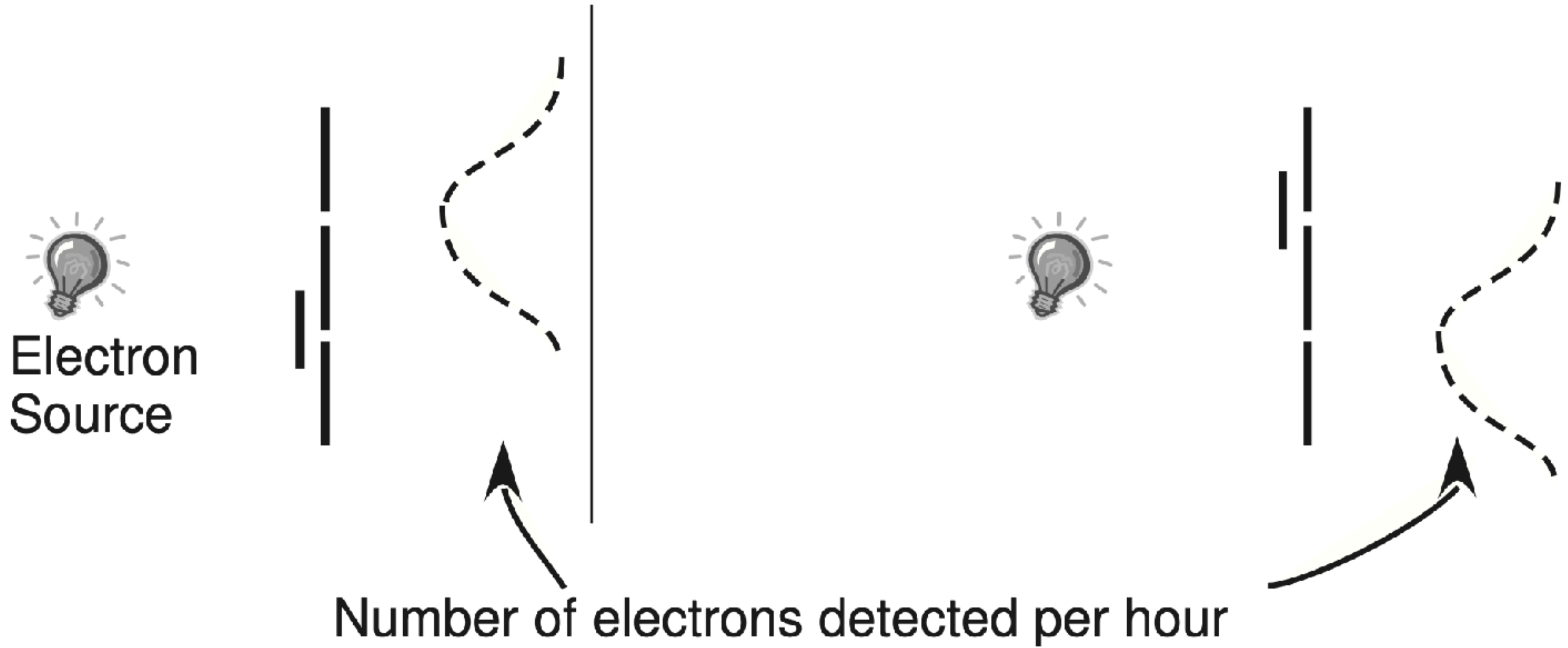


Figure 10.1 In the 2-slit experiment an electron source is placed between a wall with two slits and a detector array. When one slit is covered then, as expected, the number of electron detected is largest directly behind the open slit.

Feynman: “*negative probabilities*”

Interference

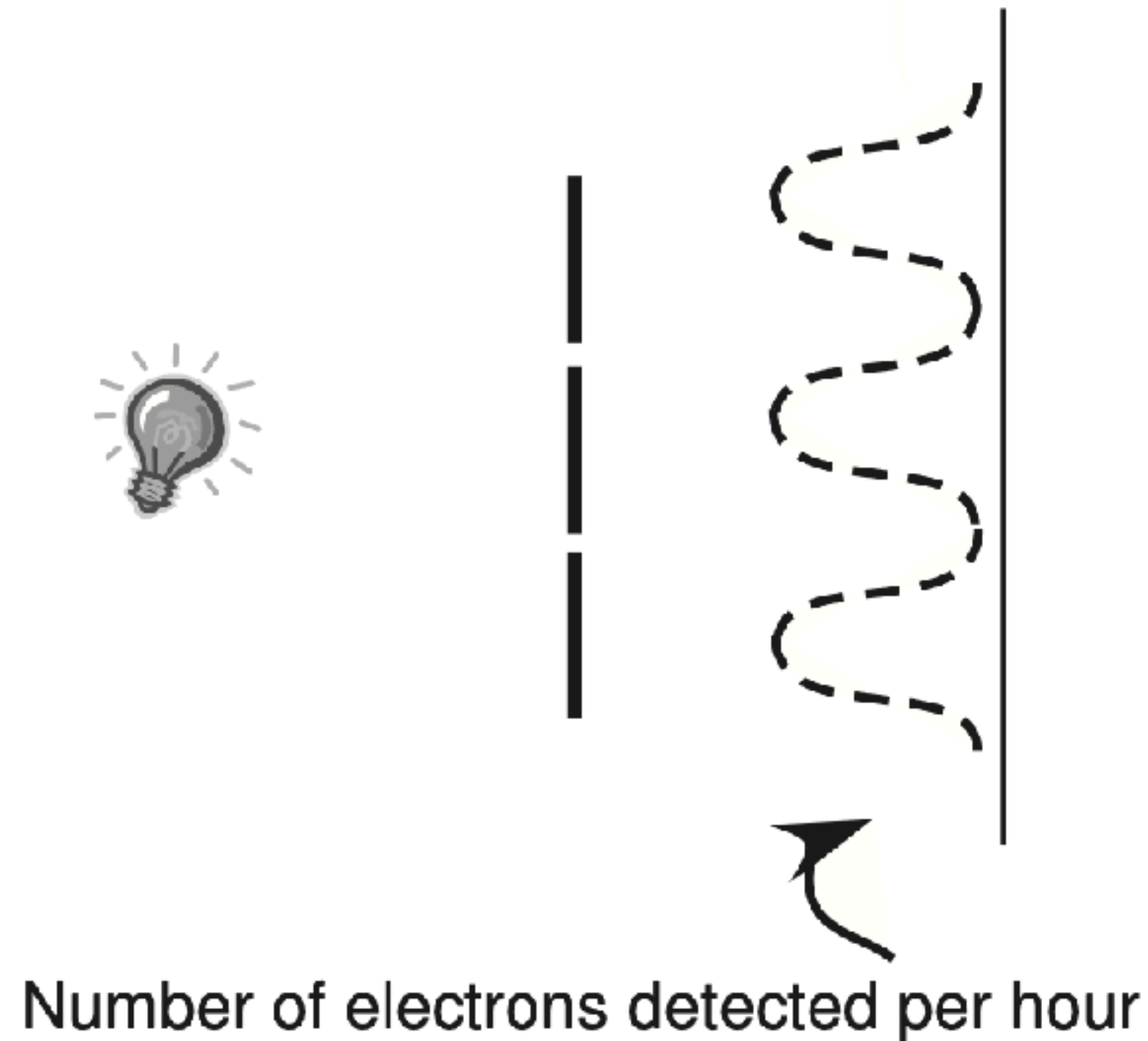
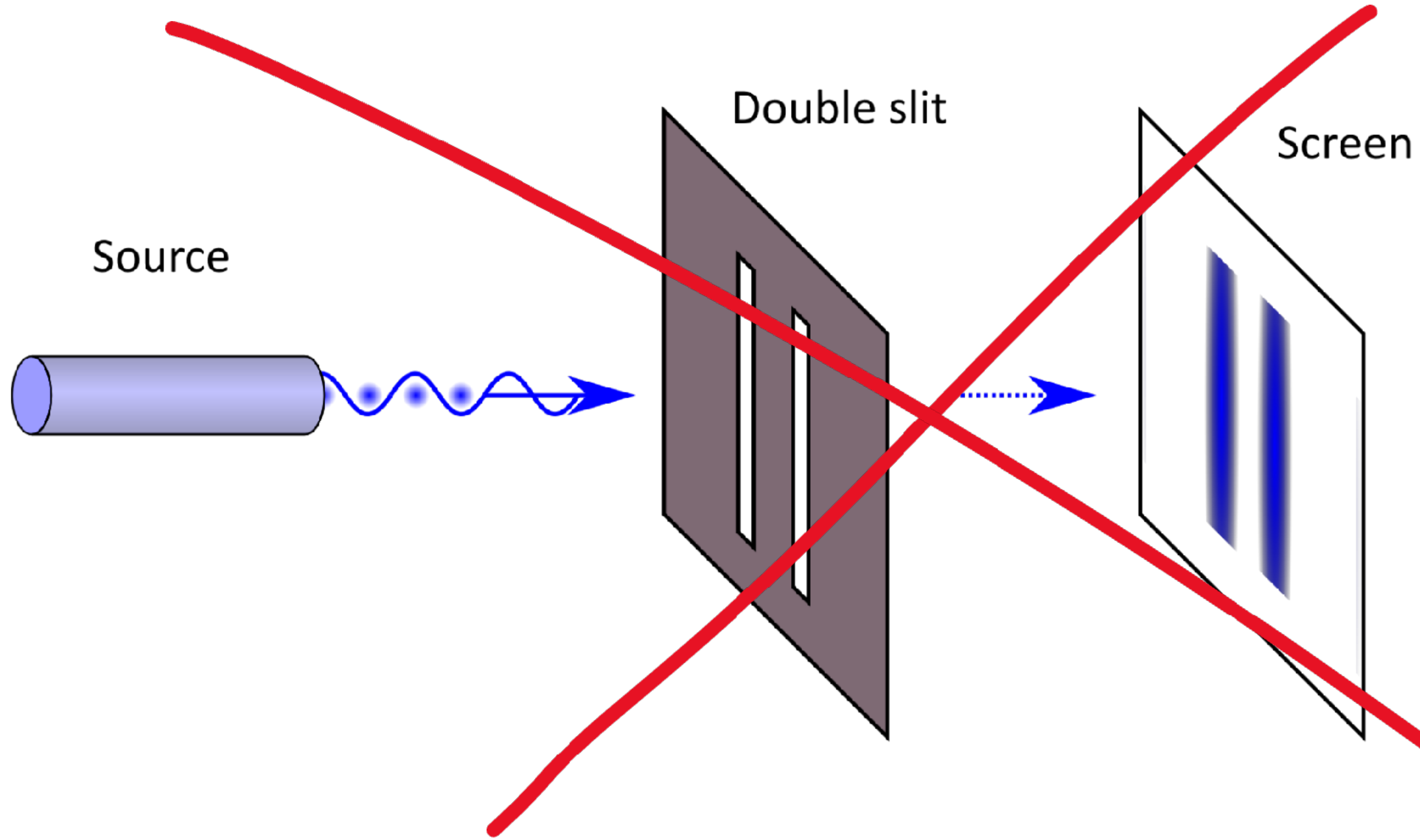
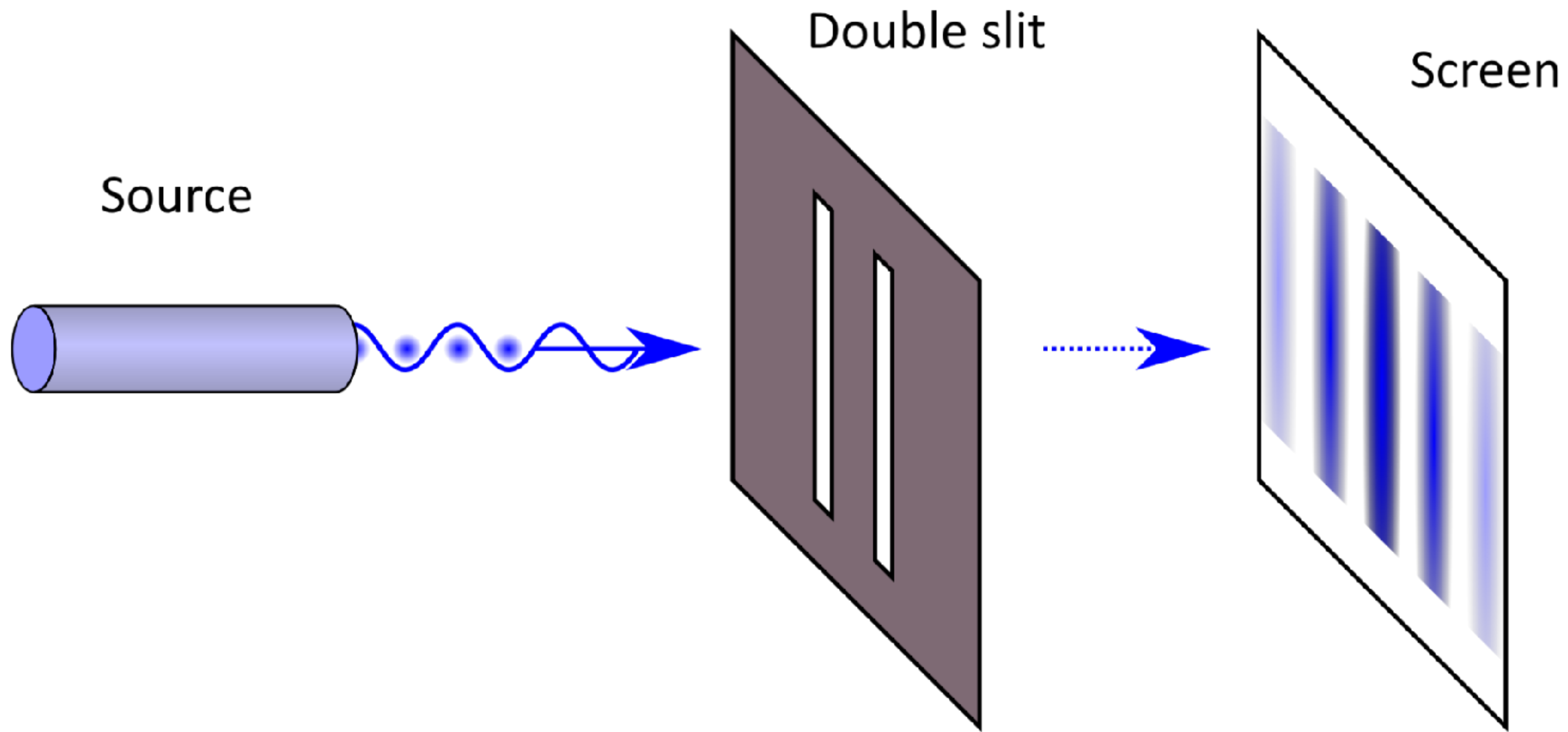
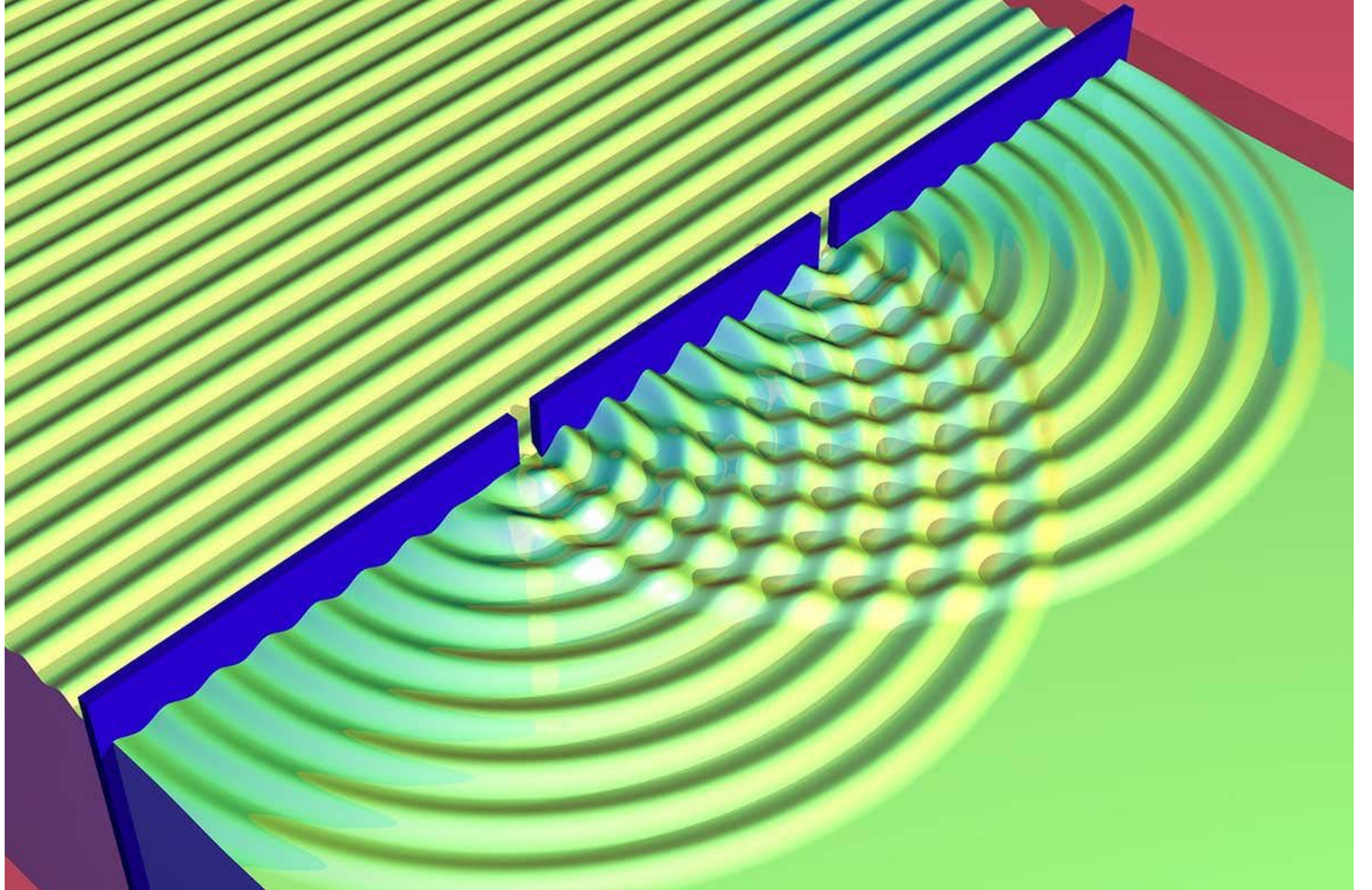


Figure 10.2 When both slits are open in the 2-slit experiment, the number of electrons detected at each position is *not the sum* of numbers when either slit is opened. There are even positions that are hit when each slit is open on its own, but are *not* hit when both slits are open.







Quantum state

1-qubit

$$a_0 \quad 0$$

$$a_1 \quad 1$$

a_0, a_1 are probability 'amplitudes'

amplitudes are complex numbers

$$a_0, a_1 \in \mathbb{C}$$

Probability from amplitude: $p = |a|^2$

Quantum state

2-qubit

a_0 00

a_1 01

a_2 10

a_3 11

Quantum state

3-qubit

a_0	000
a_1	001
a_2	010
a_3	011
a_4	100
a_5	101
a_6	110
a_7	111

Quantum state

4-qubit

a_{00}	0000
a_{01}	0001
a_{02}	0010
a_{03}	0011
a_{04}	0100
a_{05}	0101
a_{06}	0110
a_{07}	0111
a_{08}	1000
a_{09}	1001
a_{10}	1010
a_{11}	1011
a_{12}	1100
a_{13}	1101
a_{14}	1110
a_{15}	1111

Quantum state

5-qubit

```
a00 00000  
a01 00001  
a02 00010  
a03 00011  
a04 00100  
a05 00101  
a06 00110  
a07 00111  
a08 01000  
a09 01001  
a10 01010  
a11 01011  
a12 01100  
a13 01101  
a14 01110  
a15 01111  
a16 10000  
a17 10001  
a18 10010  
a19 10011  
a20 10100  
a21 10101  
a22 10110  
a23 10111  
a24 11000  
a25 11001  
a26 11010  
a27 11011  
a28 11100  
a29 11101  
a30 11110  
a31 11111
```

Quantum state

6-qubit

```
a00 000000
a01 000001
a02 000010
a03 000011
a04 000100
a05 000101
a06 000110
a07 000111
a08 001000
a09 001001
a10 001010
a11 001011
a12 001100
a13 001101
a14 001110
a15 001111
a16 010000
a17 010001
a18 010010
a19 010011
a20 010100
a21 010101
a22 010110
a23 010111
a24 011000
a25 011001
a26 011010
a27 011011
a28 011100
a29 011101
a30 011110
a31 011111
a00 100000
a01 100001
a02 100010
a03 100011
a04 100100
a05 100101
a06 100110
a07 100111
a08 101000
a09 101001
a10 101010
a11 101011
a12 101100
a13 101101
a14 101110
a15 101111
a16 110000
a17 110001
a18 110010
a19 110011
a20 110100
a21 110101
a22 110110
a23 110111
a24 111000
a25 111001
a26 111010
a27 111011
a28 111100
a29 111101
a30 111110
a31 111111
```

Quantum state 300-qubit

Length of the quantum state vector: $2^n = 2^{300} = 10^{90}$

Number of atoms in the universe: 10^{80}

Quantum state

3-qubit

a_0	000
a_1	001
a_2	010
a_3	011
a_4	100
a_5	101
a_6	110
a_7	111

Classical state

3-bit

000

001

010

011

100

101

110

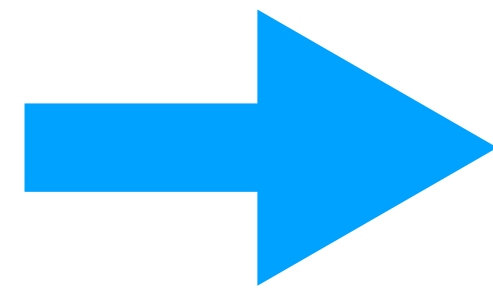
111

Classical Computation

3-bit

000
001
010
011
100
101
110
111

Computation



000
001
010
011
100
101
110
111

Computation



000
001
010
011
100
101
110
111

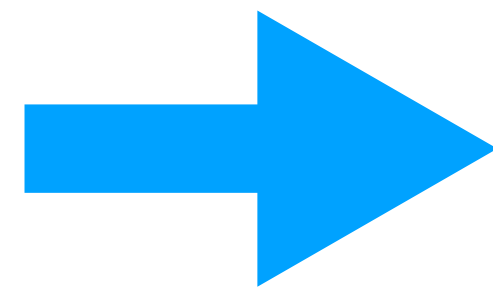
Readout

Quantum Computation

3-qubit

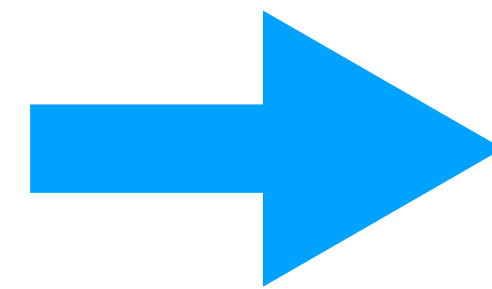
000
001
010
011
100
101
110
111

Computation



a_0 000
 a_1 001
 a_2 010
 a_3 011
 a_4 100
 a_5 101
 a_6 110
 a_7 111

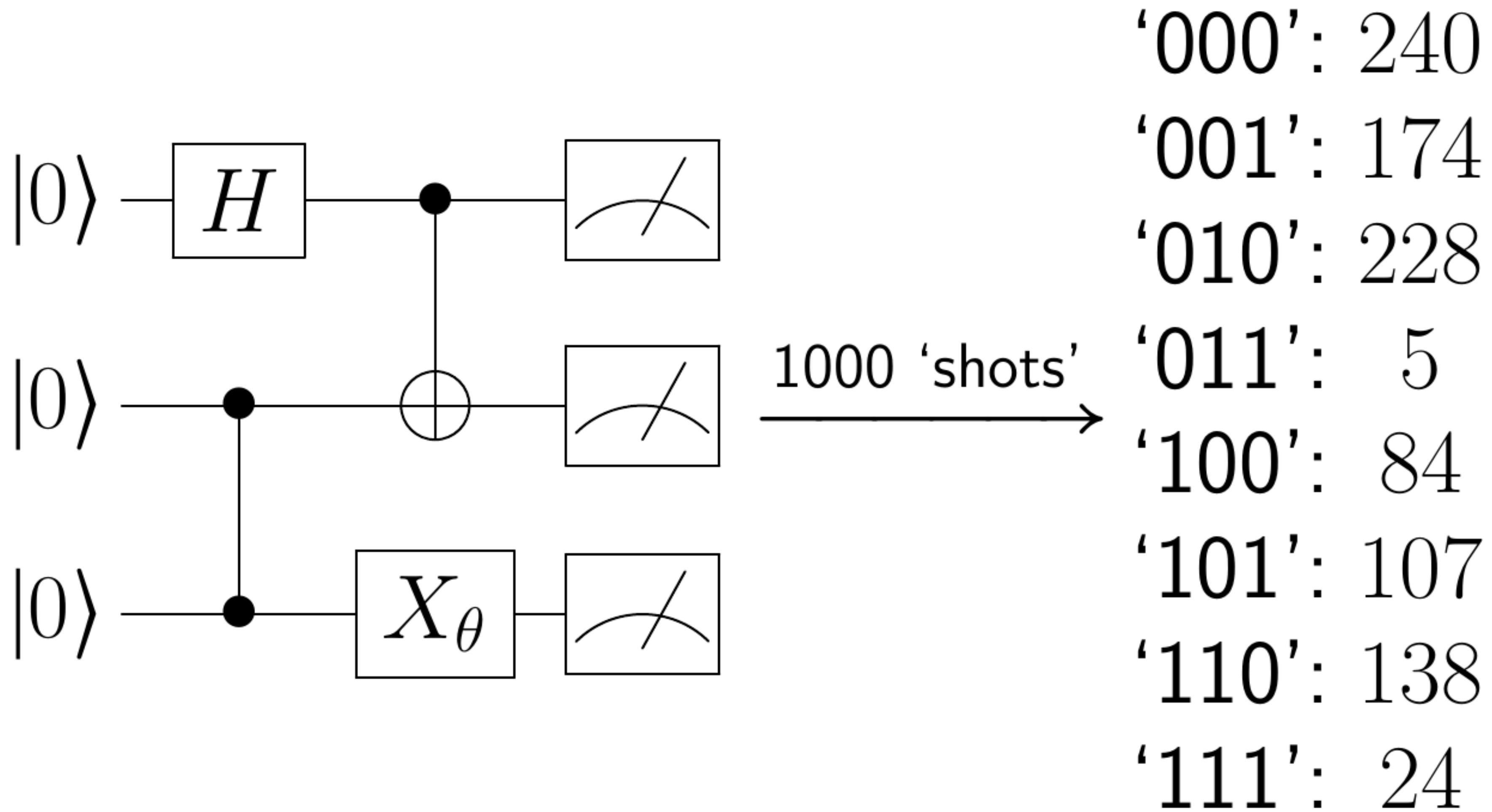
Computation



b_0 000
 b_1 001
 b_2 010
 b_3 011
 b_4 100
 b_5 101
 b_6 110
 b_7 111

Measurement

Quantum calculation (1)



Quantum calculation (2)

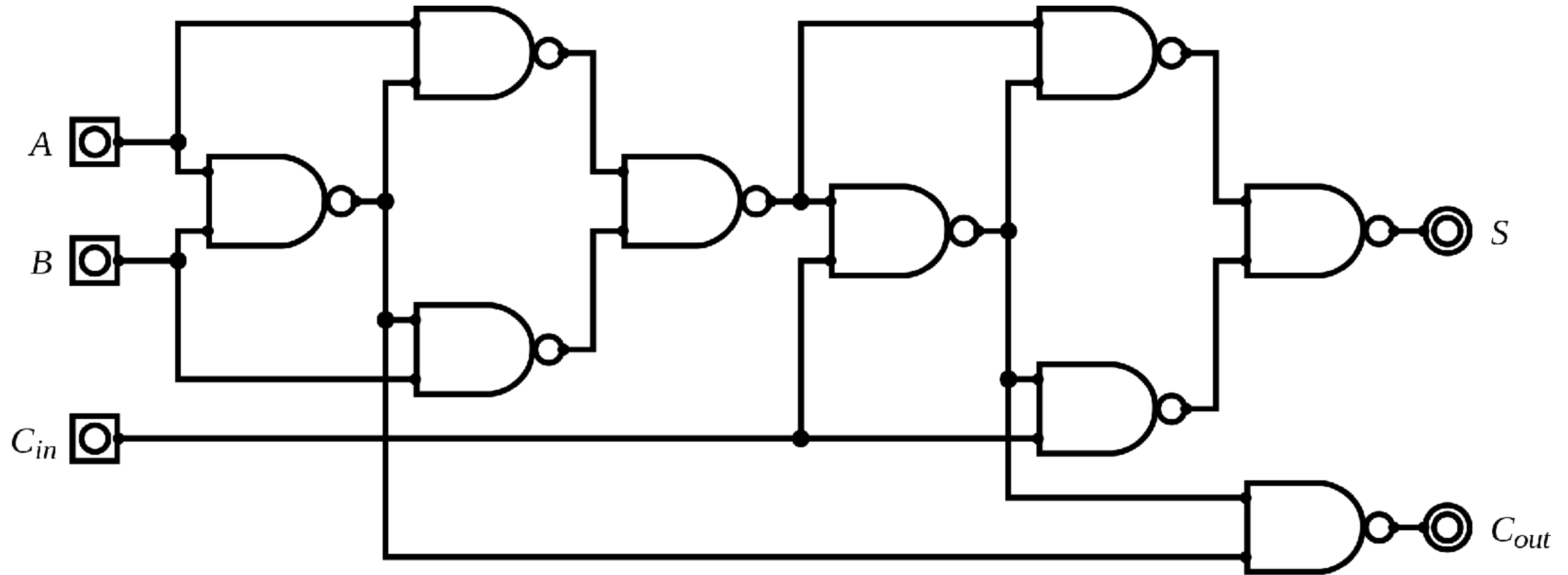
Stochastic: the result is a probability distribution

One 'shot': run a quantum circuit, measure

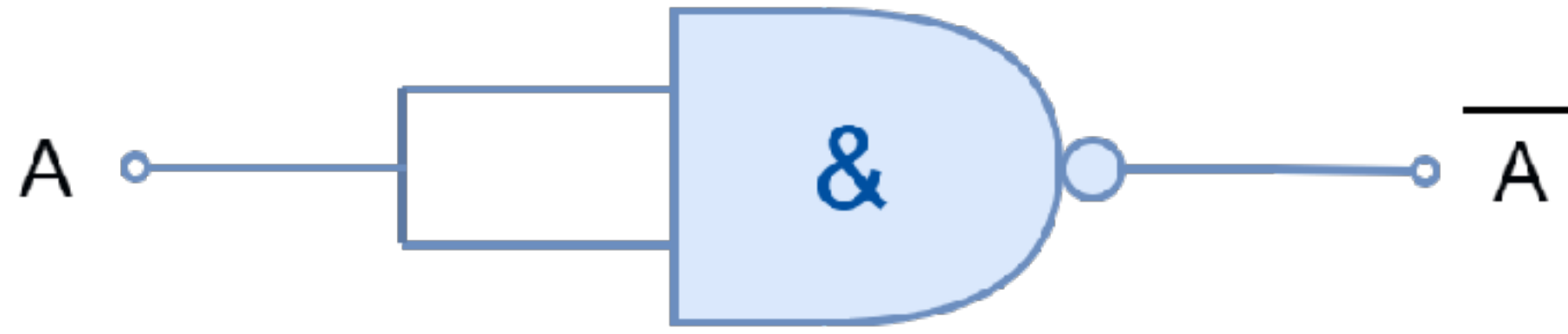
Many shots: sampling the distribution

Result: the vector of probabilities for each qubit string

Classical circuit 1940s

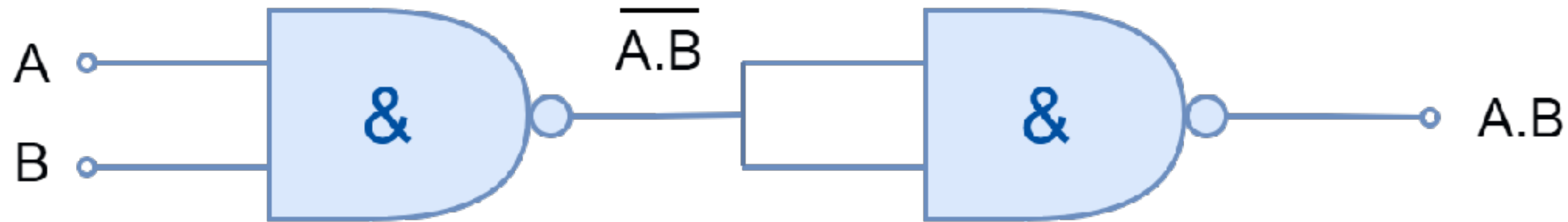


NOT Logic



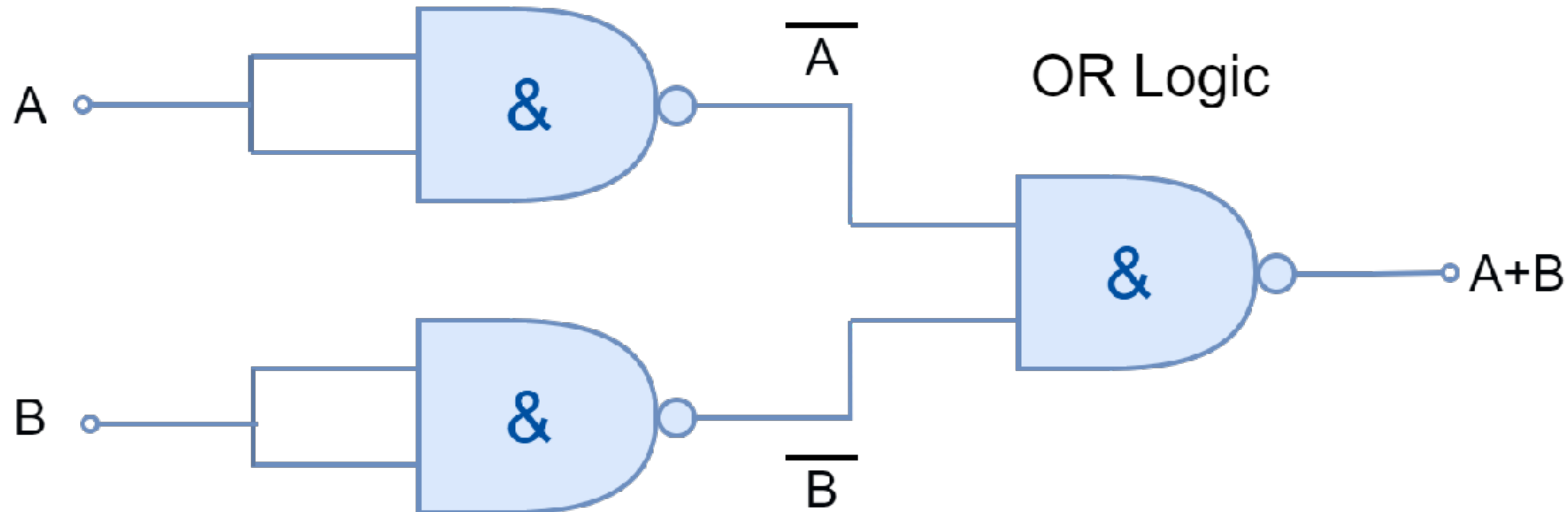
A	Q
0	1
1	0

AND Logic

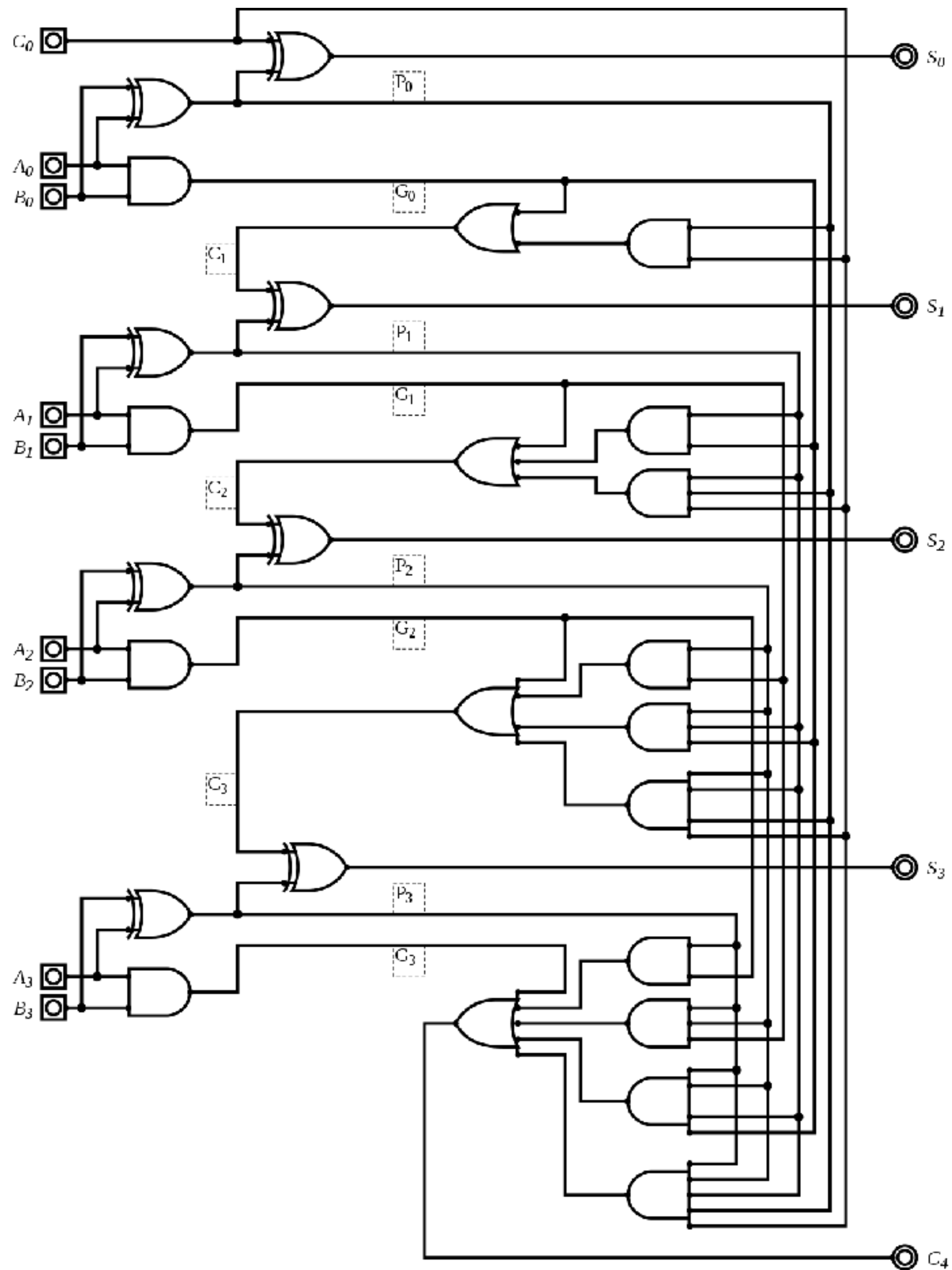


A	B	$\overline{A.B}$	Q
0	0	1	0
0	1	1	0
1	0	1	0
1	1	0	1

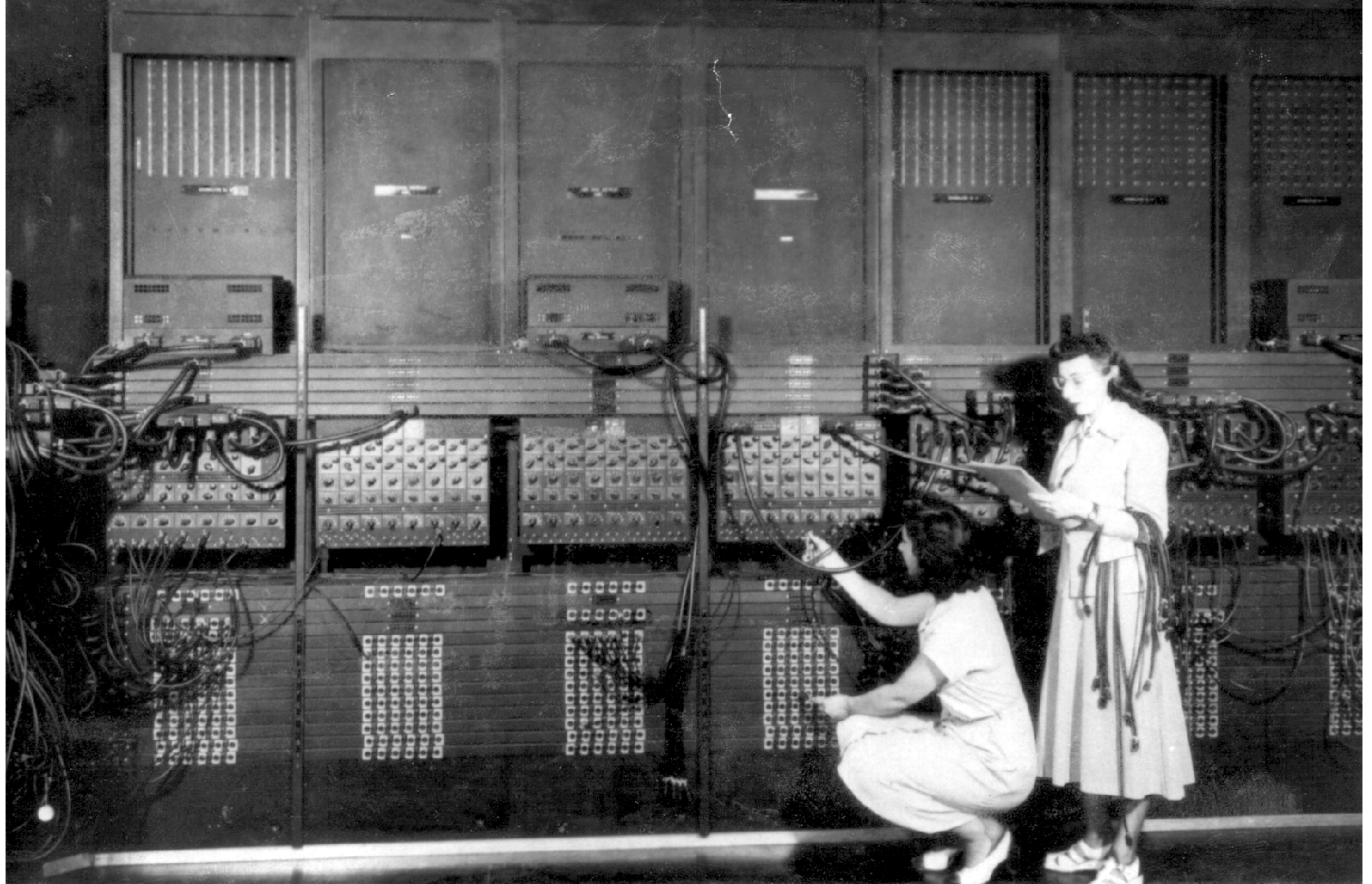
OR Logic



A	B	\overline{A}	\overline{B}	Q
0	0	1	1	0
0	1	1	0	1
1	0	0	1	1
1	1	0	0	1



**4-bit
addition**





7708

HOURS

ACCUMULATOR
NO. 8

HEATERS

OFF ON

2

3

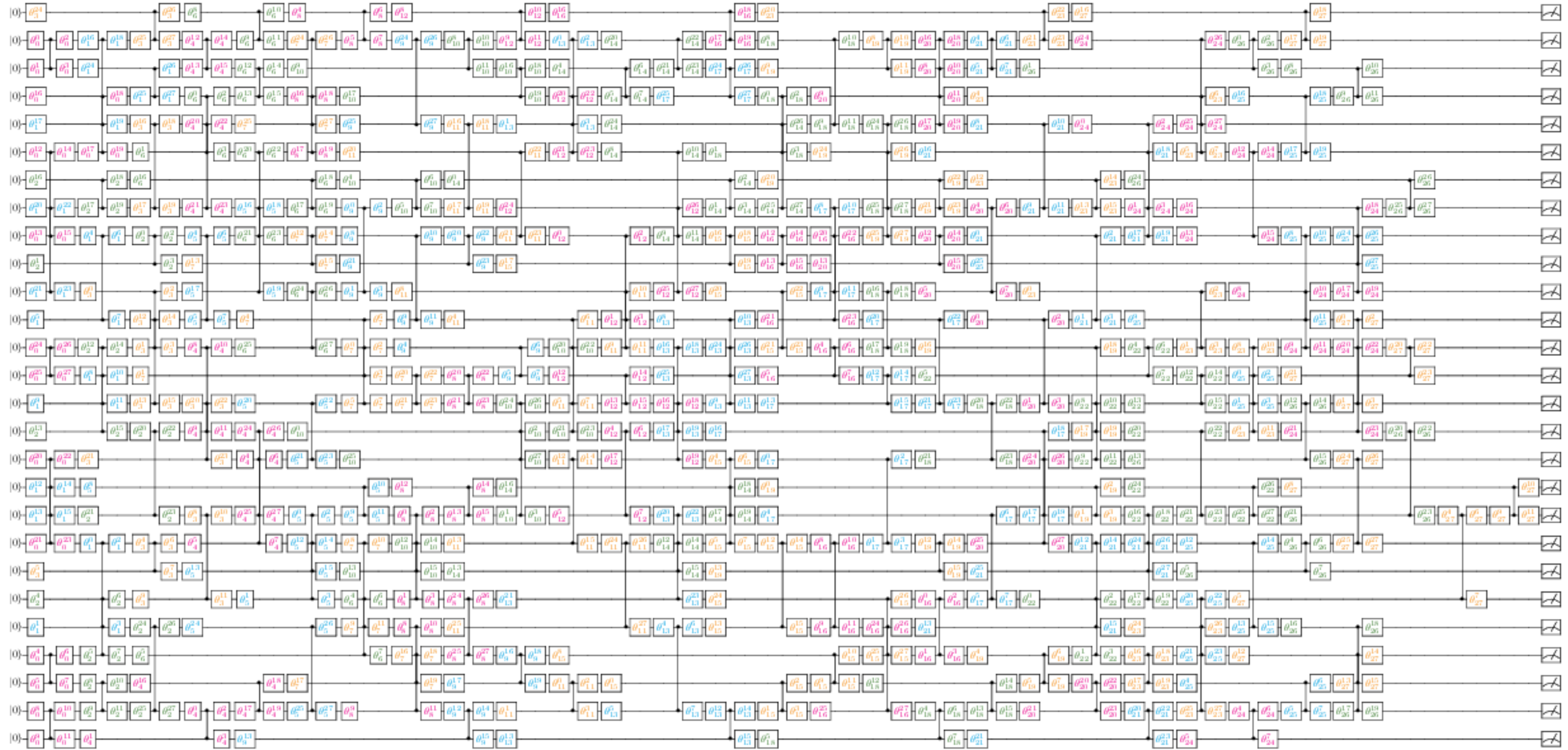
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7

8

9

27 Qubits



The future of quantum computing

Computers in the future may weigh no more than 1.5 tons

Popular Mechanics, 1949

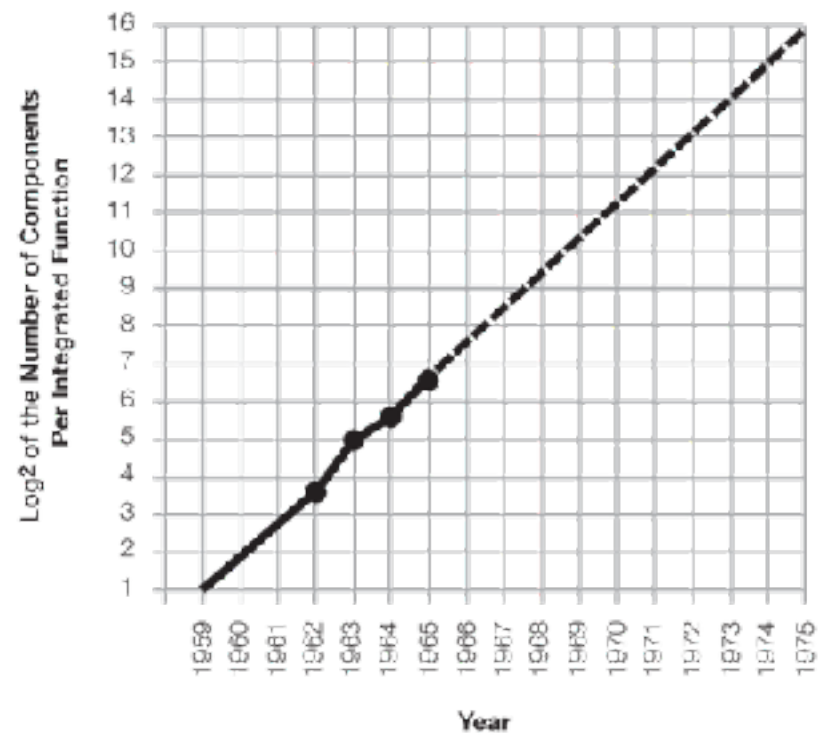


a two-mil square can also contain several kilohms of resistance or a few diodes. This allows at least 500 components per linear inch or a quarter million per square inch. Thus, 65,000 components need occupy only about one-fourth a square inch.

On the silicon wafer currently used, usually an inch or more in diameter, there is ample room for such a structure if the components can be closely packed with no space wasted for interconnection patterns. This is realistic, since efforts to achieve a level of complexity above the presently available integrated circuits are already underway using multilayer metalization patterns separated by dielectric films. Such a density of components can be achieved by present optical techniques and does not require the more exotic techniques, such as electron beam operations, which are being studied to make even smaller structures.

Increasing the yield

There is no fundamental obstacle to achieving device yields of 100%. At present, packaging costs so far exceed the cost of the semiconductor structure itself that there is no incentive to improve yields, but they can be raised as high as



is economically justified. No barrier exists comparable to the thermodynamic equilibrium considerations that often limit yields in chemical reactions; it is not even necessary to do any fundamental research or to replace present processes. Only the engineering effort is needed.

In the early days of integrated circuitry, when yields were extremely low, there was such incentive. Today ordinary integrated circuits are made with yields comparable with those obtained for individual semiconductor devices. The same pattern will make larger arrays economical, if other considerations make such arrays desirable.

Heat problem

Will it be possible to remove the heat generated by tens of thousands of components in a single silicon chip?

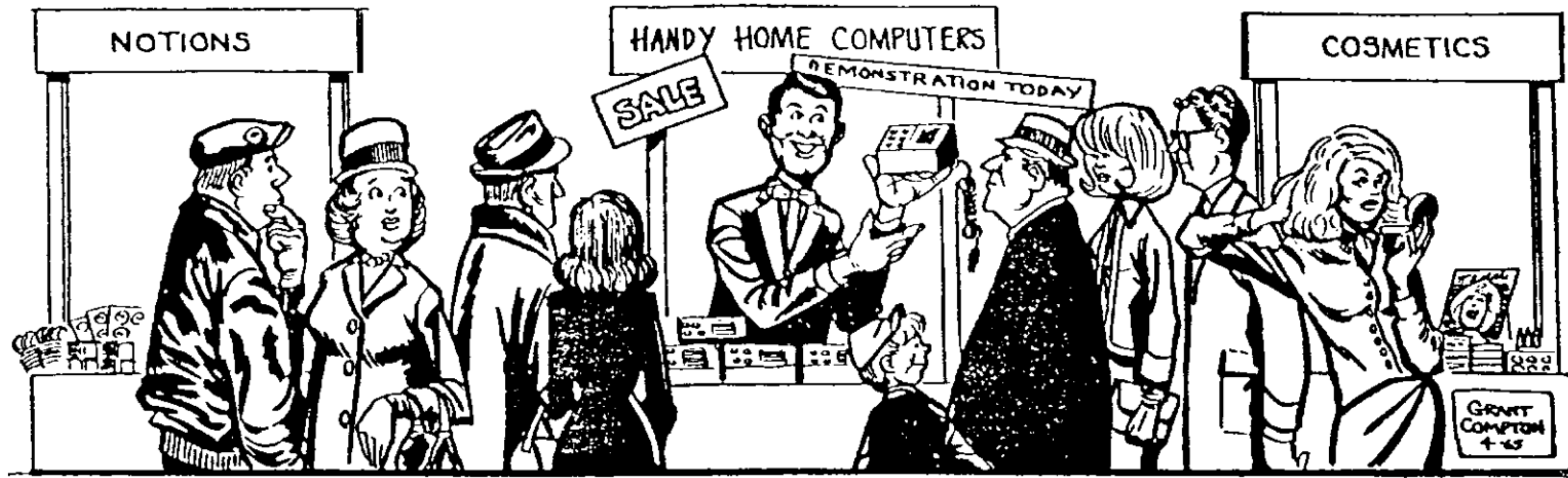
If we could shrink the volume of a standard high-speed digital computer to that required for the components themselves, we would expect it to glow brightly with present power dissipation. But it won't happen with integrated circuits. Since integrated electronic structures are two-dimensional, they have a surface available for cooling close to each center of heat generation. In addition, power is needed primarily to drive the various lines and capacitances associated with the system. As long as a function is confined to a small area on a wafer, the amount of capacitance which must be driven is distinctly limited. In fact, shrinking dimensions on an integrated structure makes it possible to operate the structure at higher speed for the same power per unit area.

Day of reckoning

Clearly, we will be able to build such component-crammed equipment. Next, we ask under what circumstances we should do it. The total cost of making a particular system function must be minimized. To do so, we could amortize the engineering over several identical items, or evolve flexible techniques for the engineering of large functions so that no disproportionate expense need be borne by a particular array. Perhaps newly devised design automation procedures could translate from logic diagram to technological realization without any special engineering.

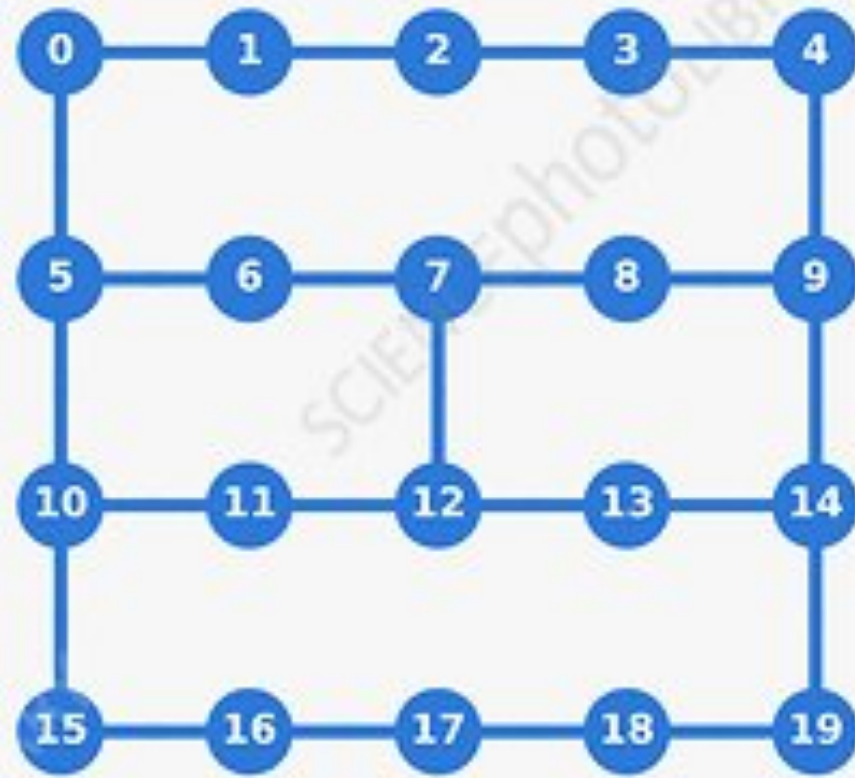
It may prove to be more economical to build large

Gordon E. Moore 1965

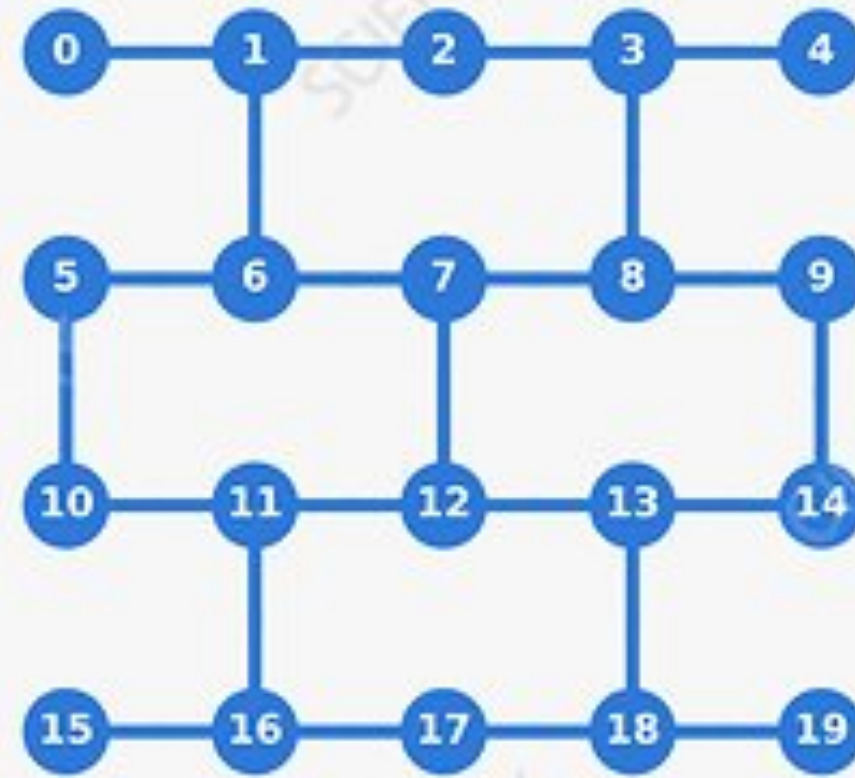


Takeaway message

- Useful quantum computers will arrive in ~2030
- Today there is no quantum software
- Few quantum computer scientists



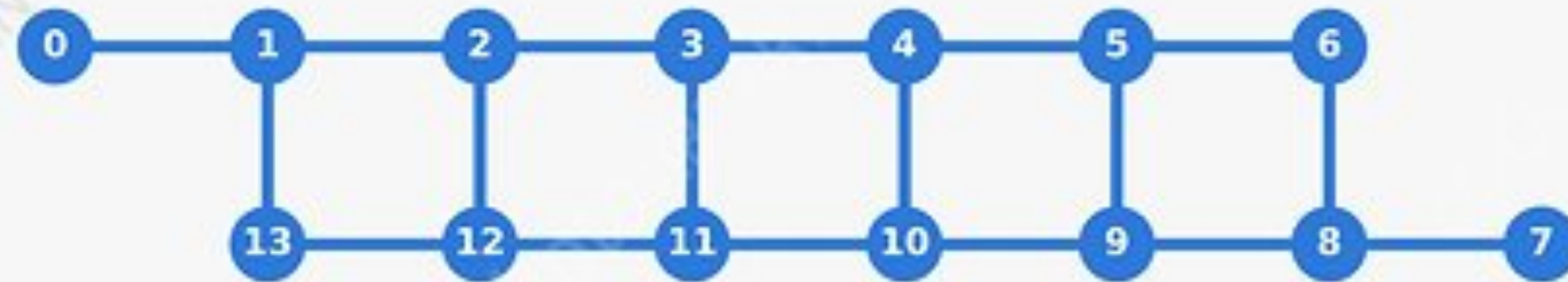
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